

Introduction

Reversed-shear tokamak configurations have some promising features for improved stability and confinement but may be unstable to Double-Tearing Modes (DTMs). Nonlinearly these instabilities can potentially cause significant plasma motion and disruptions of the annular current ring [2, 3]. Recent research has shown that equilibrium shear flows can have a stabilizing effect on both linear and nonlinear DTMs. If the rotation between the two tearing surfaces is large enough compared to the growth rate ($\Delta\omega \gtrsim \gamma$) they cannot couple linearly and the system collapses to two localized eigenmodes [6], though they may re-couple nonlinearly.

Diamagnetic drifts (characterized by the frequency ω_*) have the potential to provide both differential rotation and additional reconnection-layer stabilization [7]. Internal Transport Barriers (ITBs) with significant pressure gradients are frequently observed in reversed-shear configurations [5], suggesting ω_* effects are a likely candidate for stabilization. We extend our previous work on linear ω_* stabilization into the nonlinear regime of an $m = 2, n = 1$ DTM in cylindrical geometry using the extended MHD code MRC-3D. While we do find evidence of nonlinear stabilization, we find the effectiveness is highly dependent on the location of the pressure profile.

Equilibrium

We use the non-monotonic safety factor profile from Ref [4]:

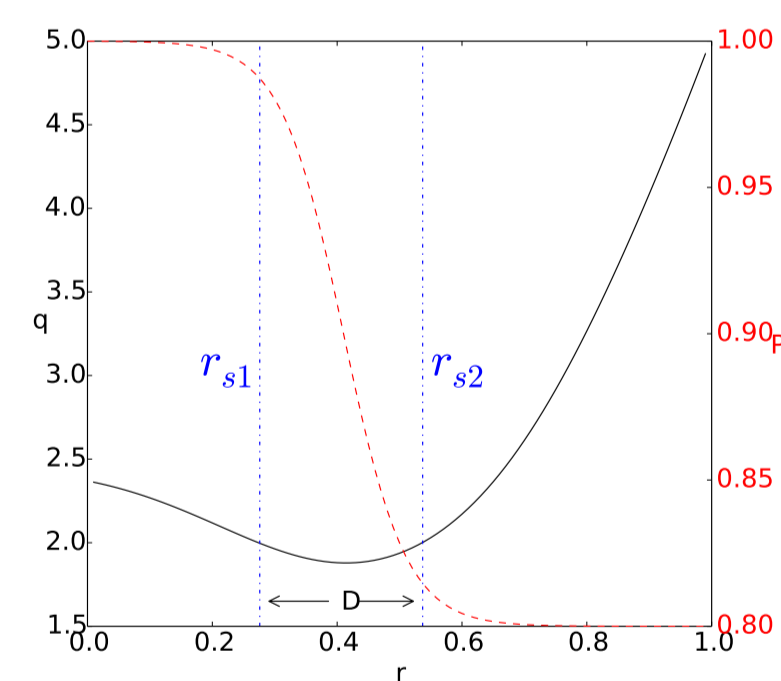
$$q(r) = q_0 F_1(r) \left\{ 1 + (r/r_0)^{2w(r)} \right\}^{1/w(r)} \quad r_0 = r_A | [m/(nq_0)]^{w(r_A)} - 1 |^{-1/2w(r_A)}$$

$$w(r) = w_0 + w_1 r^2 \quad F_1(r) = 1 + f_1 \exp \left\{ -[(r - r_{11})/r_{12}]^2 \right\}$$

with the constant values: $r_A = 0.655$, $w_0 = 3.8824$, $w_1 = 0$, $f_1 = -0.238$, $r_{11} = 0.4286$, $r_{12} = 0.304$, $m = 2$, $n = 1$. q_0 may be varied near 2.5 to change the separation D between two $q = 2$ surfaces. Assuming $B_{z0} = R_{major} = 10$ we find the in-plane field B_θ . For this work we fix $q_0 = 2.5$, giving $D \approx 0.26$. Density profiles are of the form [5]:

$$N(r) = N_0 \left\{ 1 - (1 - N_b) \frac{\tanh(r_0/\delta_N) + \tanh[(r - r_0)/\delta_N]}{\tanh(r_0/\delta_N) + \tanh[(1 - r_0)\delta_N]} \right\}$$

Where $N_0 = 1$, $r_{s1} \leq r_0 \leq r_{s2}$, and $r_{s1(2)}$ is the inner (outer) $q = 2$ surface. The parameters δ_N , N_b , and r_0 are chosen based on the desired diamagnetic drifts (ω_*) at each tearing surface. Temperature $T = 1$ is uniform.



MRC-3D Model

$$\mathbf{E} = -\mathbf{v}_i \times \mathbf{B} + \frac{d_i}{\rho} (\mathbf{J} \times \mathbf{B} - \nabla p_e) + \eta \mathbf{J} - \eta_2 \nabla^2 \mathbf{J}$$

$$\frac{\partial \rho}{\partial t} + \nabla \cdot (\rho \mathbf{v}) - D \nabla^2 \rho = 0$$

$$\frac{\partial \rho \mathbf{v}}{\partial t} + \nabla \cdot [\rho \mathbf{v} \mathbf{v} - \mathbf{B} \mathbf{B} + \mathbf{I}(p + B^2/2) - \rho \nu \nabla \mathbf{v}] = 0$$

$$\frac{\partial T_e}{\partial t} + \mathbf{v} \cdot \nabla T_e + (\gamma - 1) T_e \nabla \cdot \mathbf{v} = 0$$

$$p_s = \rho T_s, \quad p = p_e + p_i = (1 + \tau) \rho T_e$$

Where $\tau = T_i/T_e$, $\gamma = 5/3$ for an adiabatic equation of state, η is the resistivity, d_i is the ion inertial length, ν is the fluid viscosity, and D is a particle diffusivity parameter. For this work we fix $d_i = 0.1$, $\eta = 2e - 5$, and $\tau = 0$. The other dissipation parameters are given small values to aid numerical stability. Faraday's Law is used to evolve \mathbf{B} .

With these parameters, the diamagnetic drift frequency is given by:

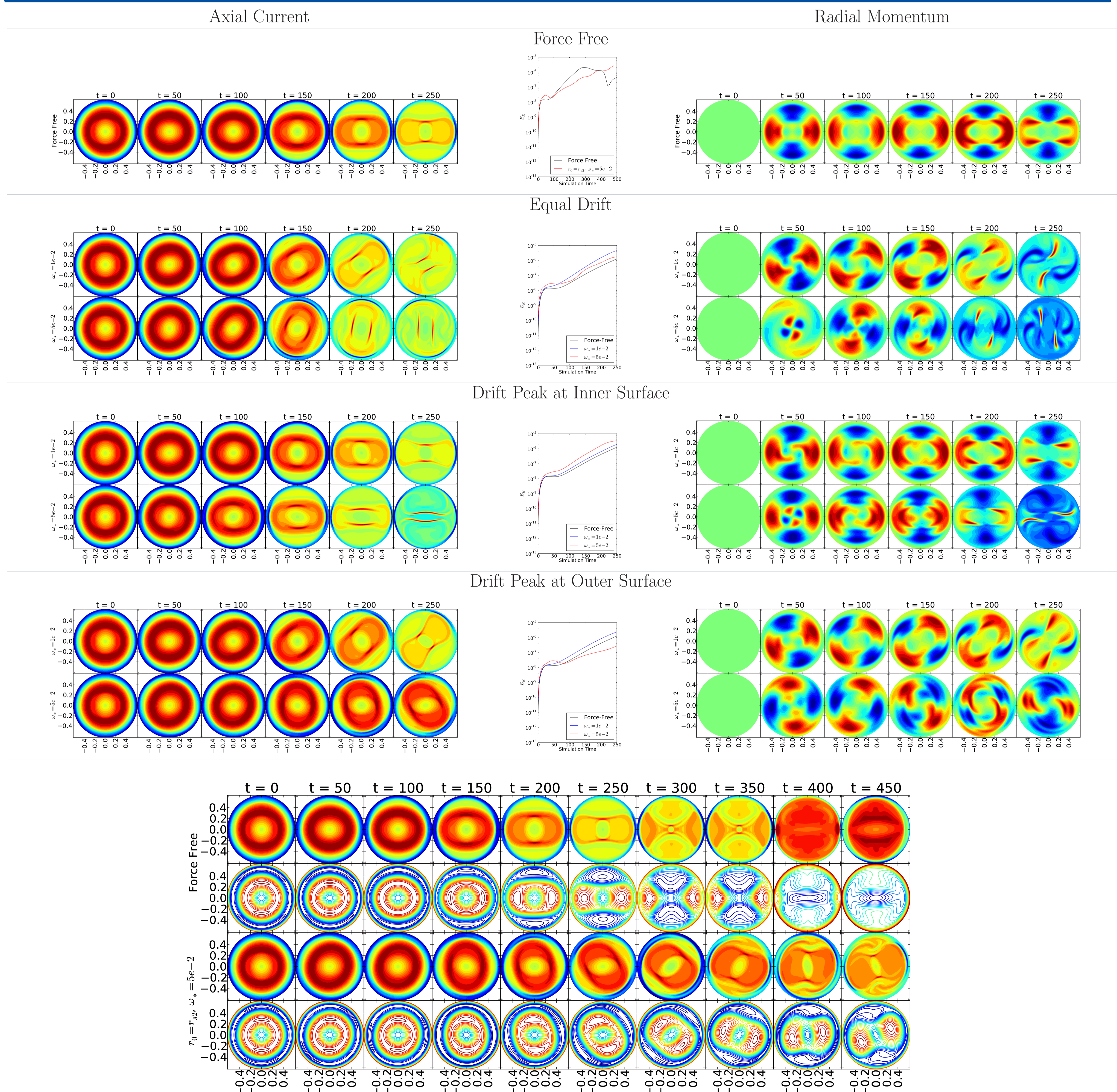
$$\omega_* = \left[d_i \frac{\nabla p_e \times \mathbf{B}}{r \rho B^2} \right]_\theta$$

Setup of Nonlinear Simulations

Based on our previous studies of this system we expect the linear decoupling threshold to lie in the range $0.01 < \Delta\omega_c < 0.05$. We use these bounds as characteristic 'coupled' and 'decoupled' states and examine them non-linearly for different locations of the peak pressure gradient. In addition to localizing the drift at the inner and outer rational surfaces, we consider a case with equal drifts at both locations to eliminate differential rotation effects.

The value of ω_* at the rational surfaces is determined by several different parameters. For this work we fix $d_i = 0.1$. The pressure profile values r_0 , δ_N , and N_b are set as follows for the three configurations of interest.

Nonlinear DTM Simulation Results



Equal Drift ω_* is equal at both surfaces. $\delta_N = 0.2$ is fixed. The parameters N_b and r_0 are set to achieve the desired drifts: $\omega = 0.01: [N_b = 0.788, r_0 = 0.455]; \omega = 0.05: [N_b = 0.298, r_0 = 0.41]$.

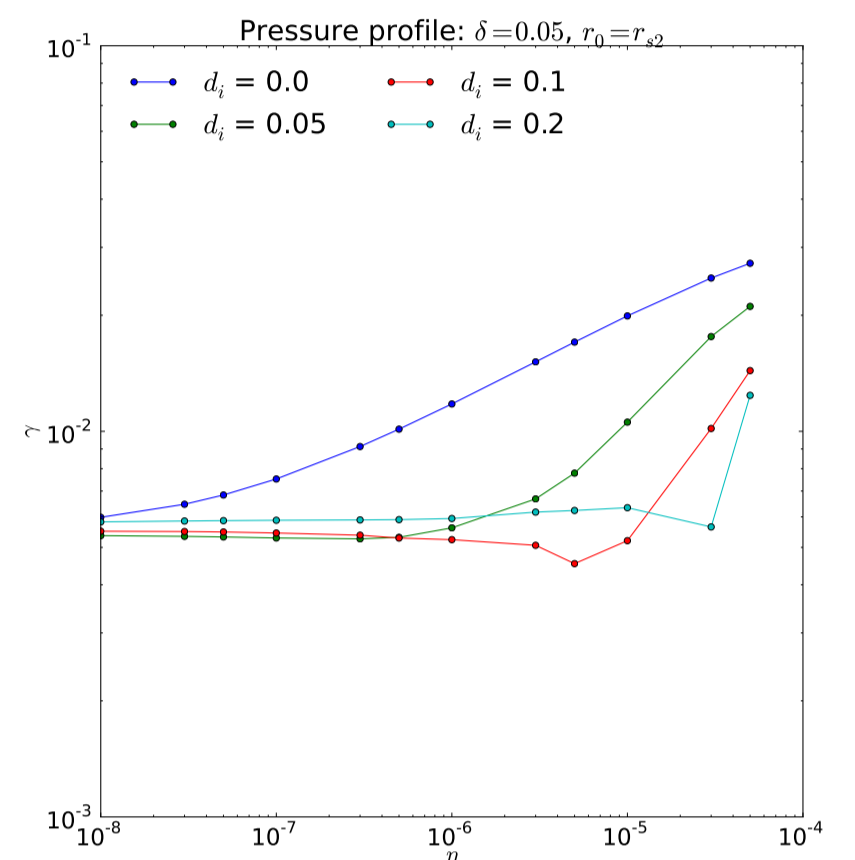
Inner Drift The pressure gradient is localized around the inner rational surface, with nearly no drift at the outer. The parameters $\delta_N = 0.1$ and $r_0 = r_{s1}$ are fixed. N_b is set to achieve the desired drifts: $\omega = 0.01: N_b = 0.948; \omega = 0.05: N_b = 0.762$.

Outer Drift The pressure gradient is localized around the outer rational surface, with nearly no drift at the inner. The parameters $\delta_N = 0.1$ and $r_0 = r_{s2}$ are fixed. N_b is set to achieve the desired drifts: $\omega = 0.01: N_b = 0.9; \omega = 0.05: N_b = 0.58$.

Linear Behavior

DTM behavior depends strongly on both the local characteristics of and coupling between the two surfaces. Some important features of the linear phase include:

- ▶ $\gamma \sim \eta^\alpha$ for $1/3 \leq \alpha \leq 3/5$ based on the coupling of the two surfaces [1].
- ▶ Flow shearing between the two surfaces can inhibit coupling and decrease the growth rate, though extremely strong shears may result in additional resonances [6].
- ▶ ω_* effects have a stabilizing effect on the mode growth despite the presence of an ideal instability caused by the pressure gradient, and shown to the right for an example profile and a range of d_i and η .



Discussion

Our results show the stabilizing effects of diamagnetic drifts on the DTM is highly dependent on where the peak of ω_* is located. A common feature of all the cases examined here is that if the modes are allowed to grow to a point where they can couple effectively the stabilizing effects are overwhelmed. Equal (or near equal) strong drifts at both rational surfaces provides some initial suppression of the mode but are extremely vulnerable to coupling, suggesting that differential rotation effects are fundamental to efficient stabilization. Locating the drift at the outer resonant surface is much more effective. It may be possible to completely suppress the outer surface with a strong enough drift, which might avoid a complete collapse of the current channel.

While many of these observations are specific to this equilibrium, these simulations show both that ω_* drifts can slow the evolution of the non-linear DTM and that the details of the pressure gradient are critically important. Conducting a similar study for modes other than the $m = 2, n = 1$ case shown here would allow for a better understanding of the ω_* effects on the 'explosive' growth phase of the DTM, which cannot easily be observed in this equilibrium. Broadening the scope of safety factor profiles may also allow a survey of experimental data where locations and strengths of ITB pressure gradients can be correlated with possible DTM driven disruptions.

References

- [1] P. L. Pritchett, et al. "Linear analysis of the double-tearing mode" *Phys. Fluids*, **23**, 1368 (1980)
- [2] Y. Ishii, et al. "Nonlinear evolution of double tearing modes" *Phys. Plasmas*, **7**, 447 (2000)
- [3] Z. X. Wang, et al. "Fast Resistive Reconnection Regime in the Nonlinear Evolution of the Double Tearing Mode" *Phys. Rev. Lett.*, **99**, 185004 (2007)
- [4] A. Bierwage, et al. "Dynamics of resistive double tearing modes with broad linear spectra" *Phys. of Plasmas*, **14**, 022107 (2007)
- [5] X. M. Zhao, et al. "Double tearing modes in the presence of internal transport barrier" *Phys. of Plasmas*, **18**, 072506 (2011)
- [6] A. Mao, et al. "Eigenmode characteristics of the double-tearing mode in the presence of shear flows" *Phys. of Plasmas*, **20**, 022114 (2013)
- [7] B. Rogers, L. Zakharov "Nonlinear ω_* -stabilization of the $m = 1$ mode in tokamaks" *Phys. Plasmas*, **2**, 3420 (1995)